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**MATHEMATICS**

**9709/11**

Paper 1 Pure Mathematics 1 (P1)

**May/June 2019**

**1 hour 45 minutes**

Candidates answer on the Question Paper.

Additional Materials: List of Formulae (MF9)

**READ THESE INSTRUCTIONS FIRST**

Write your centre number, candidate number and name in the spaces at the top of this page.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

**DO NOT WRITE IN ANY BARCODES.**

Answer **all** the questions in the space provided. If additional space is required, you should use the lined page at the end of this booklet. The question number(s) must be clearly shown.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

The use of an electronic calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [ ] at the end of each question or part question.

The total number of marks for this paper is 75.

This document consists of **21** printed pages and **3** blank pages.



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- 1 The term independent of  $x$  in the expansion of  $\left(2x + \frac{k}{x}\right)^6$ , where  $k$  is a constant, is 540.

(i) Find the value of  $k$ .

[3]

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(ii) For this value of  $k$ , find the coefficient of  $x^2$  in the expansion.

[2]

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- 2 The line  $4y = x + c$ , where  $c$  is a constant, is a tangent to the curve  $y^2 = x + 3$  at the point  $P$  on the curve.

(i) Find the value of  $c$ .

[3]

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(ii) Find the coordinates of  $P$ .

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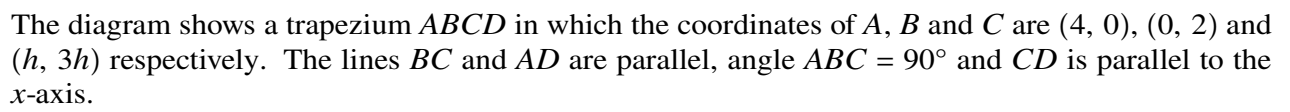
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- 3** A sector of a circle of radius  $r$  cm has an area of  $A$  cm<sup>2</sup>. Express the perimeter of the sector in terms of  $r$  and  $A$ . [4]

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- [illegible]

**[Turn over**

**5** The function  $f$  is defined by  $f(x) = -2x^2 + 12x - 3$  for  $x \in \mathbb{R}$ .

(ii) Express  $-2x^2 + 12x - 3$  in the form  $-2(x + a)^2 + b$ , where  $a$  and  $b$  are constants. [2]

[illegible]

(ii) State the greatest value of  $f(x)$ . [1]

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The function  $g$  is defined by  $g(x) = 2x + 5$  for  $x \in \mathbb{R}$ .

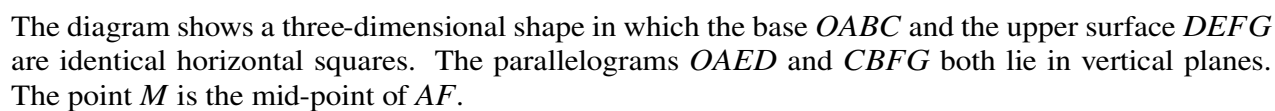
(iii) Find the values of  $x$  for which  $\text{gf}(x) + 1 = 0$ . [3]

[illegible]

**6** (i) Prove the identity  $\left(\frac{1}{\cos x} - \tan x\right)^2 \equiv \frac{1 - \sin x}{1 + \sin x}$ . [4]

This image shows a full page of a worksheet designed for handwriting practice. It consists of approximately 20 horizontal rows. Each row is defined by two parallel dotted lines, creating a series of uniform gaps for writing. The lines are evenly spaced across the entire page, providing a guide for letter height and placement. There is no text or other markings on the page.

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(i) Express each of the vectors  $\overrightarrow{AM}$  and  $\overrightarrow{GM}$  in terms of  $\mathbf{i}$ ,  $\mathbf{j}$  and  $\mathbf{k}$ . [3]

[illegible]

[illegible]

- 8** (a) The third and fourth terms of a geometric progression are 48 and 32 respectively. Find the sum to infinity of the progression. [3]

[illegible]

- (b) Two schemes are proposed for increasing the amount of household waste that is recycled each week.

Scheme *A* is to increase the amount of waste recycled each month by 0.16 tonnes.

Scheme *B* is to increase the amount of waste recycled each month by 6% of the amount recycled in the previous month.

The proposal is to operate the scheme for a period of 24 months. The amount recycled in the first month is 2.5 tonnes.

For each scheme, find the total amount of waste that would be recycled over the 24-month period. [5]

Scheme *A* .....

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Scheme *B* .....

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- 9 The function  $f$  is defined by  $f(x) = 2 - 3 \cos x$  for  $0 \leq x \leq 2\pi$ .

(i) State the range of  $f$ .

[2]

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(ii) Sketch the graph of  $y = f(x)$ .

[2]

The function  $g$  is defined by  $g(x) = 2 - 3 \cos x$  for  $0 \leq x \leq p$ , where  $p$  is a constant.

- (iii) State the largest value of  $p$  for which  $g$  has an inverse. [1]

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- (iv) For this value of  $p$ , find an expression for  $g^{-1}(x)$ . [2]

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- 10** A curve for which  $\frac{d^2y}{dx^2} = 2x - 5$  has a stationary point at (3, 6).

(i) Find the equation of the curve.

[6]

[illegible]

(ii) Find the  $x$ -coordinate of the other stationary point on the curve.

[1]

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(iii) Determine the nature of each of the stationary points.

[2]

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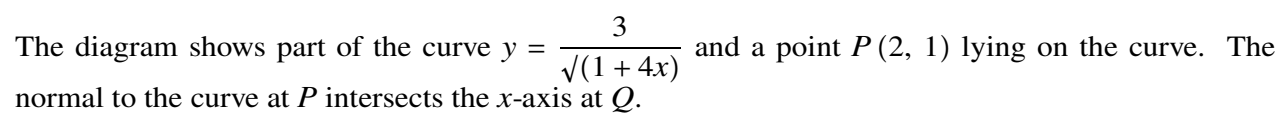
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- [illegible]

- (ii)** Find, showing all necessary working, the area of the shaded region.

[6]

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[illegible]

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